

Supplementary Material: Automatic Unsupervised Outlier Model Selection

Details on Models, Meta-features, Datasets/Testbeds, Optimization, pseudo code, and Detailed Experiment Result

A METAOD Model Set

Model set $\mathcal{M}$ is composed by pairing outlier detection algorithms to distinct hyperparameter choices. Table 2 provides a comprehensive description of models, including 302 unique models composed by 8 popular outlier detection (OD) algorithms. All models and parameters are based on the Python Outlier Detection Toolbox (PyOD)⁵.

Table 2: Outlier Detection Models; see hyperparameter definitions from PyOD [61]

Detection algorithm	Hyperparameter 1	Hyperparameter 2	Total
LOF [6]	n_neighbors: [1, 5, 10, 15, 20, 25, 50, 60, 70, 80, 90, 100]	distance: ['manhattan', 'euclidean', 'minkowski']	36
kNN [35]	n_neighbors: [1, 5, 10, 15, 20, 25, 50, 60, 70, 80, 90, 100]	method: ['largest', 'mean', 'median']	36
OCSVM [37]	nu (train error tol): [0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9]	kernel: ['linear', 'poly', 'rbf', 'sigmoid']	36
COF [45]	n_neighbors: [3, 5, 10, 15, 20, 25, 50]	N/A	7
ABOD [24]	n_neighbors: [3, 5, 10, 15, 20, 25, 50, 60, 70, 80, 90, 100]	N/A	7
iForest [31]	n_estimators: [10, 20, 30, 40, 50, 75, 100, 150, 200]	max_features: [0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9]	81
HBOS [17]	n_histograms: [5, 10, 20, 30, 40, 50, 75, 100]	tolerance: [0.1, 0.2, 0.3, 0.4, 0.5]	40
LODA [34]	n_bins: [10, 20, 30, 40, 50, 75, 100, 150, 200]	n_random_cuts: [5, 10, 15, 20, 25, 30]	54
			302

B Meta-features

B.1 Complete List of Meta-features

We summarize the meta-features used by METAOD in Table 3. When applicable, we provide the formula for computing the meta-feature(s) and corresponding variants. Some are based on [49]. Refer to the accompanied code for details.

Specifically, meta-features can be categorized into (1) statistical features, and (2) landmarker features. Broadly speaking, the former captures statistical properties of the underlying data distributions; e.g., min, max, variance, skewness, covariance, etc. of the features and feature combinations. These statistics-based meta-features have been commonly used in the AutoML literature [49].

B.2 Landmarker Meta-features

In addition to statistical meta-features, we use four OD-specific landmarker algorithms for computing OD-specific landmarker meta-features, iForest [31], HBOS [17], LODA [34], and PCA [20] (reconstruction error as outlier score), to capture outlying characteristics of a dataset. To this end, we first provide a quick overview of each algorithm and then discuss how we are using them for building meta-features. The algorithms are executed with the default parameter. Refer to the attached code for details of meta-feature construction.

Isolation Forest (iForest) [31] is a tree-based ensemble method. Specifically, iForest builds a collection of base trees using the subsampled unlabeled data, splitting on (randomly selected) features as nodes. iForest grows internal nodes until the terminal leaves contain only one sample or the predefined max depth is reached. Given the max depth is not set and we have multiple base trees with each leaf containing one sample only, the anomaly score of a sample is the aggregated depth the leaves the sample falls into. The key assumption is that an anomaly is more different than the normal samples, and is, therefore, easier to be “isolated” during the node splitting. Consequently, anomalies are closer to roots with small tree depth. For iForest, we use the balance of base trees (i.e., depth of trees and number of leaves per tree) and additional information (e.g., feature importance of each base tree). It is noted that feature importance information is available for each base tree—we therefore analyze the statistic of mean and max of base tree feature importance. Specifically, the following information of base trees are used:

⁵<https://github.com/yzhao062/pyod>

Table 3: Selected meta-features for characterizing an arbitrary dataset. See code for details.

Name	Formula	Rationale	Variants
Nr instances	n	Speed, Scalability	$\frac{n}{n}, \log(n), \log(\frac{n}{p})$
Nr features	p	Curse of dimensionality	$\log(p), \% \text{ categorical}$
Sample mean	μ	Concentration	
Sample median	$\tilde{X}$	Concentration	
Sample var	σ^2	Dispersion	
Sample min	$\max_X$	Data range	
Sample max	$\min_X$	Data range	
Sample std	σ	Dispersion	
Percentile	P_i	Dispersion	q1, q25, q75, q99
Interquartile Range (IQR)	$q75 - q25$	Dispersion	
Normalized mean	$\frac{\mu}{\max_X}$	Data range	
Normalized median	$\frac{\tilde{X}}{\max_X}$	Data range	
Sample range	$\max_X - \min_X$	Data range	
Sample Gini		Dispersion	
Median absolute deviation	$\text{median}(X - \tilde{X})$	Variability and dispersion	
Average absolute deviation	$\text{avg}(X - \tilde{X})$	Variability and dispersion	
Quantile Coefficient Dispersion	$\frac{(q75 - q25)}{(q75 + q25)}$	Dispersion	
Coefficient of variance		Dispersion	
Outlier outside 1 & 99	$\% \text{ samples outside } 1\% \text{ or } 99\%$	Basic outlying patterns	
Outlier 3 STD	$\% \text{ samples outside } 3\sigma$	Basic outlying patterns	
Normal test	If a sample differs from a normal dist.	Feature normality	
k th moments			5th to 10th moments
Skewness	Feature skewness	Feature normality	min, max, μ, σ , skewness, kurtosis
Kurtosis	$\frac{\mu_4}{\sigma^4}$	Feature normality	min, max, μ, σ , skewness, kurtosis
Correlation	ρ	Feature interdependence	min, max, μ, σ , skewness, kurtosis
Covariance	Cov	Feature interdependence	min, max, μ, σ , skewness, kurtosis
Sparsity	$\frac{\# \text{Unique values}}{n}$	Degree of discreteness	min, max, μ, σ , skewness, kurtosis
ANOVA p-value	p_{ANOVA}	Feature redundancy	min, max, μ, σ , skewness, kurtosis
Coeff of variation	$\frac{\sigma}{\mu}$	Dispersion	
Norm. entropy	$\frac{H(X)}{\log_2 n}$	Feature informativeness	min, max, σ, μ
Landmarker (HBOS)	See §B.2	Outlying patterns	Histogram density
Landmarker (LODA)	See §B.2	Outlying patterns	Histogram density
Landmarker (PCA)	See §B.2	Outlying patterns	Explained variance ratio, singular values
Landmarker (iForest)	See §B.2	Outlying patterns	# of leaves, tree depth, feature importance

- *Tree depth*: min, max, mean, std, skewness, and kurtosis
- *Number of leaves*: min, max, mean, std, skewness, and kurtosis
- *Mean of base tree feature importance*: min, max, mean, std, skewness, and kurtosis
- *Max of base tree feature importance*: min, max, mean, std, skewness, and kurtosis

Histogram-based Outlier Scores (HBOS) [17] assumes that each dimension (feature) of the datasets is independent. It builds a histogram on each feature to calculate the density. Given there are n samples and d features, for each histogram from $1 \dots d$, HBOS estimates the sample density using all n samples. Intuitively, the anomaly score of sample g is defined as the sum of log of inverse density. In other words, it can be considered as an aggregation of density estimation on each feature. Obviously, the samples falling in high-density areas are more likely to be normal points and vice versa. The following information is included as part of METAOD:

- *Mean of each histogram (per feature)*: min, max, mean, std, skewness, and kurtosis
- *Max of each histogram (per feature)*: min, max, mean, std, skewness, and kurtosis

Lightweight on-line detector of anomalies (LODA) [34] is a fast ensemble-based anomaly detection algorithm. It shares a similar idea as HBOS—"although one one-dimensional histogram is a very weak anomaly detector, their collection yields to a strong detector". Different from HBOS that simply aggregates over all independent histograms, LODA extends the histogram-based model generating k random projection vectors to compress data into one-dimensional space for building histograms. Similar to HBOS, we include in the following information as part of meta-features:

- *Mean of each random projection (per feature)*: min, max, mean, std, skewness, and kurtosis
- *Max of each random projection (per feature)*: min, max, mean, std, skewness, and kurtosis
- *Mean of each histogram (per feature)*: min, max, mean, std, skewness, and kurtosis
- *Max of each histogram (per feature)*: min, max, mean, std, skewness, and kurtosis

Principal component analysis based outlier detector (PCA) [20] aims to quantify sample outlyingness by projecting them into lower dimensions through principal component analysis. Since the

number of normal samples is much bigger than the number of outliers, the identified projection matrix is mainly suited for normal samples. Consequently, the reconstruction error of normal samples are smaller than that of outlier samples, which can be used to measure sample outlyingness. For PCA, we include the following information into meta-features:

- *Explained variance ratio on the first three principal components*: The percentage of variance it captures for the top 3 principal components
- *Singular values*: The top 3 singular values generated during SVD process

Additionally, we also leverage the **outlier scores by OD landmarks** after appropriate scaling, e.g., normalization/standardization.

C Gradient Derivations

In this section we provide the details for the gradient derivation of METAOD. It is organized as follow. We first provide a quick overview of gradient derivation in classical recommender systems, and then show the derivation of the rank-based criterion used in METAOD.

C.1 Background

Given a rating matrix $\mathbf{P} \in \mathbb{R}^{n \times m}$ with n users rating on m items, $\mathbf{P}_{ij}$ denotes i th user's rating on the j th item in classical recommender system setting. For learning the latent factors in k dimensions, we try to factorize $\mathbf{P}$ into user matrix $\mathbf{U} \in \mathbb{R}^{n \times k}$ and the item matrix $\mathbf{V} \in \mathbb{R}^{d \times k}$ to make $\mathbf{P} \approx \mathbf{UV}^T$.

In classical matrix factorization setting, some entries of the performance matrix $\mathbf{P}$ is missing. Consequently, one may use stochastic gradient descent to minimize the mean squared error (MSE) between $\mathbf{P}$ and $\mathbf{UV}^T$ through all non-empty entries. For each rating $\mathbf{P}_{ij}$, the loss L is defined as:

$$L_{i,j} = L(\mathbf{U}_i, \mathbf{V}_j^T) = (\mathbf{P}_{ij} - \mathbf{U}_i \mathbf{V}_j^T)^2 \quad (9)$$

The total loss over all non-empty entries is:

$$L = \sum_{i,j} (\mathbf{P}_{ij} - \mathbf{U}_i \mathbf{V}_j^T)^2 \quad (10)$$

The optimization process iterates over all non-empty entries of the performance matrix $\mathbf{P}$, and updates $\mathbf{U}_i$ and $\mathbf{V}_j$ using the learning rate η as:

$$\mathbf{U}_i \leftarrow \mathbf{U}_i - \eta \frac{\partial L}{\partial \mathbf{U}_i} \quad (11)$$

$$\mathbf{V}_j \leftarrow \mathbf{V}_j - \eta \frac{\partial L}{\partial \mathbf{V}_j} \quad (12)$$

C.2 Gradient Derivation for DCG-based Criterion

As we aim to maximize the total *dataset-wise* DCG, we make a pass over meta-train datasets one by one at each epoch as shown in Algorithm 1. We update $\mathbf{U}_i$ and $\mathbf{V}_j$ by gradient descent as shown below. It is noted that predicted performance of j th model on i th dataset is defined as the dot product of corresponding dataset and model vector: $\hat{\mathbf{P}}_{ij} = \mathbf{U}_i \mathbf{V}_j^T$. So Eq. (5) can be rearranged as:

$$\begin{aligned}
-\text{sDCG}_i &= \sum_{j=1}^m \frac{b^{\mathbf{P}_{ij}} - 1}{\log_2(1 + \sum_{k=1}^m \sigma(\hat{\mathbf{P}}_{ik} - \hat{\mathbf{P}}_{ij}))} \\
&= \ln(2) \sum_{j=1}^m \frac{b^{\mathbf{P}_{ij}} - 1}{\ln(1 + \sum_{k=1}^m \sigma(\mathbf{U}_i \mathbf{V}_k^T - \mathbf{U}_i \mathbf{V}_j^T))} \\
&= \ln(2) \sum_{j=1}^m \frac{b^{\mathbf{P}_{ij}} - 1}{\ln(1 + \sigma(0) + \sum_{k \neq j} \sigma(\mathbf{U}_i \mathbf{V}_k^T - \mathbf{U}_i \mathbf{V}_j^T))} \\
&= \ln(2) \sum_{j=1}^m \frac{b^{\mathbf{P}_{ij}} - 1}{\ln(\frac{3}{2} + \sum_{k \neq j} \sigma(\mathbf{U}_i \mathbf{V}_k^T - \mathbf{U}_i \mathbf{V}_j^T))} \\
&= \ln(2) \sum_{j=1}^m \frac{b^{\mathbf{P}_{ij}} - 1}{\ln(\frac{3}{2} + \sum_{k \neq j} \sigma(\mathbf{U}_i \mathbf{V}_k^T - \mathbf{U}_i \mathbf{V}_j^T))} \tag{13}
\end{aligned}$$

$$\tag{14}$$

We compute the gradient of $\mathbf{U}_i$ and $\mathbf{V}_j^T$ as the partial derivative of $-\text{sDCG}_i$ as shown in Eq. (13). To ease the notation, we define

$$w_{jk}^i = \mathbf{U}_i \mathbf{V}_k^T - \mathbf{U}_i \mathbf{V}_j^T = \langle \mathbf{U}_i, (\mathbf{V}_k - \mathbf{V}_j) \rangle \tag{15}$$

$$\beta_j^i = \frac{3}{2} + \sum_{k \neq j} \sigma(\mathbf{U}_i \mathbf{V}_k^T - \mathbf{U}_i \mathbf{V}_j^T) = \frac{3}{2} + \sum_{k \neq j} \sigma(w_{jk}^i) \tag{16}$$

By plugging Eq. (15) and (16) back into Eq. (13), it is simplified into

$$-\text{sDCG}_i = \ln(2) \sum_{j=1}^m \frac{b^{\mathbf{P}_{ij}} - 1}{\ln(\frac{3}{2} + \sum_{k \neq j} \sigma(\mathbf{U}_i \mathbf{V}_k^T - \mathbf{U}_i \mathbf{V}_j^T))} = \ln(2) \sum_{j=1}^m \frac{b^{\mathbf{P}_{ij}} - 1}{\ln(\beta_j^i)} \tag{17}$$

$$\tag{18}$$

We then obtain the gradients of $\mathbf{U}_i$ and $\mathbf{V}_j^T$ as follows:

$$\frac{\partial L}{\partial \mathbf{U}_i} = \frac{\partial(-\text{sDCG}_i)}{\partial \mathbf{U}_i} = \ln(2) \frac{\partial \left(\sum_{j=1}^m \frac{b^{\mathbf{P}_{ij}} - 1}{\ln(\beta_j^i)} \right)}{\partial \mathbf{U}_i} \tag{19}$$

$$= \ln(2) \sum_{j=1}^m \left[\frac{b^{\mathbf{P}_{ij}} - 1}{\beta_j^i \ln^2(\beta_j^i)} \sum_{k \neq j} \sigma(w_{jk}^i) (1 - \sigma(w_{jk}^i)) (\mathbf{V}_k - \mathbf{V}_j) \right] \tag{20}$$

$$\frac{\partial L}{\partial \mathbf{V}_j} = \frac{\partial(-\text{sDCG}_i)}{\partial \mathbf{V}_j} = \ln(2) \frac{\partial \left(\sum_{j=1}^m \frac{b^{\mathbf{P}_{ij}} - 1}{\ln(\beta_j^i)} \right)}{\partial \mathbf{U}_i} \tag{21}$$

$$= -\ln(2) \sum_{j=1}^m \left[\frac{b^{\mathbf{P}_{ij}} - 1}{\beta_j^i \ln^2(\beta_j^i)} \sum_{k \neq j} \sigma(w_{jk}^i) (1 - \sigma(w_{jk}^i)) \mathbf{U}_i \right] \tag{22}$$

D METAOD Pseudo Code

Algorithm 1 provides detailed steps of METAOD, for both offline (meta-learning) and online (model selection) stages.

Algorithm 1 METAOD: Offline and Online Phases

Input: (Offline) meta-train database $\mathcal{D}_{\text{train}}$, model set $\mathcal{M}$, latent dimension k ; (Online) new OD dataset $\mathbf{X}_{\text{test}}$

Output: (Offline) Meta-learner for OD model selection; (Online) Selected model for $\mathbf{X}_{\text{test}}$

► (Offline) OD Meta-learner Training (§3.2.1)

- 1: Train & evaluate $\mathcal{M}$ on $\mathcal{D}_{\text{train}}$ to get performance matrix $\mathbf{P}$
- 2: Extract meta-features (§3.3), $\mathbf{M} := \psi(\{\mathbf{X}_1, \dots, \mathbf{X}_n\})$
- 3: Init. $\mathbf{U}^{(0)}$ by embedding meta-features, $\mathbf{U}^{(0)} := \phi(\mathbf{M}; k)$
- 4: Init. $\mathbf{V}^{(0)}$ by standard normal dist. $\mathbf{V}^{(0)} \sim \mathcal{N}(0, 1)$
- 5: **while** not converged **do** ► alternate. opt. by SGD, (§3.4)
- 6: Shuffle dataset order in $\mathcal{D}_{\text{train}}$
- 7: **for** $i = 1, \dots, n$ **do**
- 8: Update $\mathbf{U}_i$ by Eq. (7)
- 9: **for** $j = 1, \dots, m$ **do**
- 10: Update $\mathbf{V}_j$ by Eq. (8)
- 11: **end for**
- 12: **end for**
- 13: **end while**
- 14: Train f regressing $\phi(\mathbf{M}; k)$ onto $\mathbf{U}$ (at convergence)
- 15: **Save** extractors ψ , embed. ϕ , regressor f , $\mathbf{V}$ (at conv.)

► (Online) OD Model Selection (§3.2.2)

- 16: Extract meta-features, $\mathbf{M}_{\text{test}} := \psi(\mathbf{X}_{\text{test}})$
- 17: Get latent vector after embedding, $\mathbf{U}_{\text{test}} := f(\phi(\mathbf{M}_{\text{test}}))$
- 18: Predict model set performance, $\mathbf{P}_{\text{test}} := \mathbf{U}_{\text{test}} \mathbf{V}^T$
- 19: **Return** $\arg \max_j \mathbf{P}_{\text{test}}(j)$ as the selected model for $\mathbf{X}_{\text{test}}$

E Dataset Description and Testbed Setup

E.1 POC Testbed Setup

POC testbed is built to simulate the testbed when meta-train and test datasets come from similar distribution. Model selection on test data can therefore benefit from the prior experience on the train set. For this purpose, we use the benchmark datasets⁶ [11]. In short, they adapt 19 datasets from UCI repository and also create a synthetic dataset to make a pool of 20 “mothersets”. For each motherset, they first separate anomalies from normal points, and then generate “childsets” from the motherset by sampling and controlling outlying properties: (i) point difficulty; (ii) relative frequency, i.e., the number of anomalies; (iii) clusteredness and (iv) feature irrelevance. Taking this approach, the childsets generated from the same motherset with the same properties are deemed to be “siblings” with high similarity. Refer to the original paper for details of the data generation process.

We build the POC testbed by selecting five siblings from each motherset, resulting in 100 datasets. For robustness, we split the 100 datasets into 5 folds for cross-validation. Each fold contains 20 independent datasets with no siblings, and the corresponding train set (80 datasets) contain their siblings. Refer to the code for the 100 randomly selected childsets for POC testbed.

E.2 ST Testbed Setup

Different from the setting of POC, ST testbed aims to test out METAOD’s performance *in the wild*, i.e. when train and test datasets are all independent with limited similarity.

⁶<https://ir.library.oregonstate.edu/concern/datasets/47429f155>

To build the ST testbed, we combine the datasets from three different sources resulting in 62 independent datasets as shown in Table 4: (i) 23 datasets from ODDS Library⁷; (ii) 19 datasets DAMI datasets [8]⁸ as well as (iii) 20 benchmark datasets⁶ [11] used in POC. For ST testbed, we run leave-one-out cross validation. That is, each time 61 datasets are used for meta-train and the remaining one for test.

F Baselines: Detailed Description

The 10 baseline methods are organized into three categories:

(i) *No model selection* always employs either the same model, specifically the popular LOF or iForest detector, or the ensemble of all the models:

- **Local outlier factor (LOF)** [6] is a popular OD method that measures a sample’s deviation in the local region regarding its neighbors.
- **Isolation Forest (iForest)** [31] is a SOTA tree ensemble that measures the difficulty of “isolating” a sample via randomized splits in feature space.
- **Mega Ensemble (ME)** averages outlier scores from the 302 models for a given dataset. ME does not perform model selection but rather uses *all* the models.

(ii) *Simple meta-learners* pick the generally well-performing model, globally or locally:

- **Global Best (GB)** is the *simplest meta-learner* that selects the model with the largest avg. performance across all train datasets, *without* using meta-features.
- **ISAC** [23] clusters the meta-train datasets based on meta-features. Given a new dataset, it identifies its closest cluster and selects the best model with largest avg. performance on the cluster’s datasets.
- **ARGOSMART (AS)** [33] finds the closest meta-train dataset (1NN) to a given test dataset, based on meta-feature similarity, and selects the model with the best performance on the 1NN dataset.

(iii) *Optimization-based meta-learners* learn meta-feature based task similarities toward optimizing performance estimates:

- **Supervised Surrogates (SS)** [55]: Given the meta-train datasets, it directly maps the meta-features onto model performances by regression.
- **ALORS** [32] factorizes the performance matrix to latent factors, and estimates performance as dot product of the latent factors. A non-linear regressor maps meta-features onto latent factors.
- $\dagger$ METAOD_C is a variant: performance and meta-feature matrices are concatenated as $\mathbf{C} = [\mathbf{P}, \mathbf{M}] \in \mathbb{R}^{n \times (m+d)}$, before factorization, $\mathbf{C} \approx \mathbf{U}\mathbf{V}^T$. Given a new dataset, zero-concatenated meta-features are projected and reconstructed as $[\hat{\mathbf{P}}_{\text{new}}; \hat{\mathbf{M}}_{\text{new}}] = [0 \dots 0; \mathbf{M}_{\text{new}}]\mathbf{V}\mathbf{V}^T$.
- $\dagger$ METAOD_F is a variant, where $\mathbf{U}$ is fixed at $\phi(\mathbf{M})$ after the embedding step; only $\mathbf{V}$ is optimized.

Additionally, we report **Empirical Upper Bound (EUB)** (only applicable to POC): Recall that each POC dataset has 4 “siblings” from the same motherset with similar outlying properties. We consider the performance of the best model on a dataset’s “siblings” as its EUB, as siblings provide significant information as to which models are suitable. Note that this (valuable) information is generally not available in practice—hence serves as an upper bound. As for ST with lower task similarity, we include **Random Selection (RS)** as a baseline to quantify how the methods compare to random.

G Additional Experiment Results

G.1 Experiment Results for POC Testbed

We present the performances of compared methods in Table 5, and hypothesis test results in Table 6. It is noted these results are averaged across five folds. The results shows that METAOD achieves the best MAP among all meta-learners.

⁷<http://odds.cs.stonybrook.edu>

⁸<http://www.dbs.ifi.lmu.de/research/outlier-evaluation/DAMI>

Table 4: ST testbed composed by ODDS library (23 datasets), DAMI library (19 datasets), and Emmott benchmark (20 datasets)

	Data	Pts	Dim	% Outlier
1	annthyroid (ODDS)	7200	6	7.4167
2	arrhythmia (ODDS)	452	274	14.6018
3	breastw (ODDS)	683	9	34.9927
4	glass (ODDS)	214	9	4.2056
5	ionosphere (ODDS)	351	33	35.8974
6	letter (ODDS)	1600	32	6.25
7	lympho (ODDS)	148	18	4.0541
8	mammography (ODDS)	11183	6	2.325
9	mnist (ODDS)	7603	100	9.2069
10	musk (ODDS)	3062	166	3.1679
11	optdigits (ODDS)	5216	64	2.8758
12	pendigits (ODDS)	6870	16	2.2707
13	pima (ODDS)	768	8	34.8958
14	satellite (ODDS)	6435	36	31.6395
15	satimage-2 (ODDS)	5803	36	1.2235
16	shuttle (ODDS)	49097	9	7.1511
17	smtp_n (ODDS)	95156	3	0.0315
18	speech (ODDS)	3686	400	1.6549
19	thyroid (ODDS)	3772	6	2.4655
20	vertebral (ODDS)	240	6	12.5
21	vowels (ODDS)	1456	12	3.4341
22	wbc (ODDS)	378	30	5.5556
23	wine (ODDS)	129	13	7.7519
24	Annthroid (DAMI)	7129	21	7.4905
25	Arrhythmia (DAMI)	450	259	45.7778
26	Cardiotocography (DAMI)	2114	21	22.0435
27	HeartDisease (DAMI)	270	13	44.4444
28	Hepatitis (DAMI)	80	19	16.25
29	InternetAds (DAMI)	1966	1555	18.7182
30	PageBlocks (DAMI)	5393	10	9.4567
31	Pima (DAMI)	768	8	34.8958
32	SpamBase (DAMI)	4207	57	39.9097
33	Stamps (DAMI)	340	9	9.1176
34	Wilt (DAMI)	4819	5	5.3331
35	ALOI (DAMI)	49534	27	3.0444
36	Glass (DAMI)	214	7	4.2056
37	PenDigits (DAMI)	9868	16	0.2027
38	Shuttle (DAMI)	1013	9	1.2833
39	Waveform (DAMI)	3443	21	2.9044
40	WBC (DAMI)	223	9	4.4843
41	WDBC (DAMI)	367	30	2.7248
42	WPBC (DAMI)	198	33	23.7374
43	abalone_1231 (Emmott)	1986	15	5.0352
44	comm.and.crime_0936 (Emmott)	910	404	1.0989
45	concrete_1096 (Emmott)	468	32	1.0684
46	fault_0246 (Emmott)	278	38	17.9856
47	gas_0321 (Emmott)	6000	128	0.1
48	imgseg_1526 (Emmott)	1320	25	10
49	landsat_1761 (Emmott)	230	36	10
50	letter.rec_1666 (Emmott)	4089	23	10.0024
51	magic.gamma_1411 (Emmott)	6000	22	5
52	opt.digits_1316 (Emmott)	3180	248	5
53	pageb_0126 (Emmott)	733	14	16.2347
54	particle_1336 (Emmott)	6000	200	5
55	shuttle_0071 (Emmott)	6000	20	16.3167
56	skin_1706 (Emmott)	6000	4	10
57	spambase_0681 (Emmott)	2522	57	0.5155
58	synthetic_1786 (Emmott)	329	14	10.0304
59	wave_0661 (Emmott)	3024	21	0.5291
60	wine_0611 (Emmott)	3720	24	0.5108
61	yeast_1221 (Emmott)	926	8	5.0756
62	yearp_0231 (Emmott)	6000	202	48.6

Table 5: Method evaluation in POC testbed (average precision). The most performing method is highlighted in **bold**. The rank is provided in parenthesis (lower ranks denote better performance). METAOD achieves the best average precision and average rank among all meta-learners.

Dataset	LOF	iForest	ME	GB	ISAC	AS	SS	ALORS	MetaOD_C	MetaOD_F	MetaOD	EUB
abalone	0.0812 (12)	0.1679 (10)	0.1441 (11)	0.1738 (9)	0.192 (6)	0.229 (3)	0.224 (4)	0.1747 (8)	0.1815 (7)	0.2141 (5)	0.2329 (2)	0.2394 (1)
comm.and.crime	0.0839 (10)	0.0913 (8)	0.0797 (11)	0.0855 (9)	0.0638 (12)	0.1001 (5)	0.1122 (2)	0.099 (7)	0.1079 (3)	0.0999 (6)	0.1072 (4)	0.1156 (1)
concrete	0.0297 (2)	0.0279 (3)	0.0298 (1)	0.0251 (5)	0.0224 (7)	0.022 (8)	0.0279 (3)	0.0236 (6)	0.0131 (12)	0.0198 (9)	0.0185 (10)	0.0147 (11)
fault	0.1898 (12)	0.3755 (7)	0.323 (10)	0.3735 (8)	0.197 (11)	0.3949 (2)	0.3778 (5)	0.3723 (9)	0.4217 (1)	0.3813 (4)	0.3768 (6)	0.3899 (3)
gas	0.0193 (5)	0.0031 (11)	0.0083 (8)	0.0033 (10)	0.0059 (9)	0.0481 (1)	0.0152 (6)	0.0024 (12)	0.0392 (2)	0.013 (7)	0.0229 (4)	0.0387 (3)
imgseq	0.1153 (12)	0.3618 (6)	0.2586 (11)	0.3598 (9)	0.3659 (5)	0.3514 (10)	0.3891 (4)	0.3605 (8)	0.3612 (7)	0.3989 (3)	0.408 (2)	0.4166 (1)
landsat	0.1644 (4)	0.1306 (9)	0.131 (8)	0.13 (10)	0.1071 (12)	0.1578 (5)	0.138 (7)	0.1111 (11)	0.1844 (1)	0.1562 (6)	0.1784 (3)	0.1844 (1)
letter.rec	0.1529 (7)	0.0986 (11)	0.112 (9)	0.0991 (10)	0.0946 (12)	0.222 (2)	0.218 (5)	0.1168 (8)	0.2216 (3)	0.2229 (1)	0.2179 (6)	0.2216 (3)
magic.gamma	0.1152 (9)	0.1303 (4)	0.1104 (10)	0.1314 (3)	0.1096 (11)	0.1319 (2)	0.1299 (5)	0.1294 (6)	0.102 (12)	0.1255 (8)	0.1263 (7)	0.1351 (1)
opt.digits	0.0662 (9)	0.0668 (7)	0.0603 (12)	0.0665 (8)	0.0742 (3)	0.0795 (2)	0.0689 (6)	0.0606 (11)	0.0705 (4)	0.066 (10)	0.0701 (5)	0.0803 (1)
pageb	0.3956 (11)	0.4581 (6)	0.3801 (12)	0.4574 (7)	0.4384 (9)	0.4829 (3)	0.4616 (5)	0.4621 (4)	0.4281 (10)	0.4498 (8)	0.4898 (2)	0.4939 (1)
particle	0.0546 (12)	0.0782 (5)	0.0626 (11)	0.0746 (8)	0.0761 (6)	0.1 (1)	0.0936 (3)	0.0739 (9)	0.0683 (10)	0.0867 (4)	0.0757 (7)	0.0982 (2)
shuttle	0.2015 (11)	0.2058 (9)	0.1935 (12)	0.2056 (10)	0.2961 (5)	0.3165 (3)	0.2711 (7)	0.2105 (8)	0.3165 (3)	0.2932 (6)	0.3225 (1)	0.3185 (2)
skin	0.1161 (9)	0.0926 (11)	0.0995 (10)	0.0911 (12)	0.1814 (6)	0.165 (8)	0.2408 (4)	0.1737 (7)	0.2808 (1)	0.2808 (1)	0.2808 (1)	0.2278 (5)
spambase	0.0187 (12)	0.0713 (9)	0.0571 (11)	0.0706 (10)	0.0873 (6)	0.0744 (8)	0.1292 (1)	0.0757 (7)	0.0981 (4)	0.112 (2)	0.0942 (5)	0.0982 (3)
synthetic	0.1233 (4)	0.1226 (5)	0.1157 (8)	0.1132 (11)	0.154 (1)	0.1218 (6)	0.1147 (10)	0.1151 (9)	0.1468 (3)	0.1182 (7)	0.1483 (2)	0.1046 (12)
wave	0.0577 (9)	0.0114 (12)	0.0297 (10)	0.0117 (11)	0.2925 (8)	0.3413 (5)	0.3486 (1)	0.3244 (7)	0.3486 (1)	0.344 (4)	0.3365 (6)	0.3486 (1)
wine	0.0082 (11)	0.0087 (5)	0.0084 (10)	0.0085 (8)	0.0085 (8)	0.0073 (12)	0.0087 (5)	0.0124 (2)	0.0097 (3)	0.0086 (7)	0.0088 (4)	0.0129 (1)
yeast	0.0813 (2)	0.0781 (4)	0.073 (8)	0.0762 (6)	0.0796 (3)	0.068 (11)	0.0781 (4)	0.0693 (9)	0.0885 (1)	0.067 (12)	0.0733 (7)	0.0688 (10)
yearp	0.4894 (5)	0.4911 (4)	0.4862 (7)	0.4913 (3)	0.4703 (12)	0.4716 (10)	0.4916 (2)	0.4891 (6)	0.4716 (10)	0.4741 (9)	0.4801 (8)	0.4937 (1)
average	0.1282 (8.7)	0.1536 (7.4)	0.1382 (9.7)	0.1524 (8.35)	0.1658 (7.6)	0.1943 (5.49)	0.197 (4.95)	0.1728 (7.6)	0.198 (4.9)	0.1966 (5.95)	0.2035 (4.48)	0.2051 (3.2)
STD	0.1219	0.1487	0.1294	0.1489	0.1386	0.1491	0.1486	0.1487	0.1485	0.1530	0.1587	0.156

Table 6: Pairwise statistical test results between METAOD and baselines by Wilcoxon signed rank test in POC. Statistically better method shown in **bold** (both marked **bold** if no significance). METAOD related pairs are surrounded by rectangles. METAOD (MAP=0.2035) is statistically significantly better than baselines including LOF (0.1282), iForest (0.1536), ME (0.1382), GB (0.1524), ISAC (0.1658), and ALORS (0.1728), and comparable to EUB (0.2051), the empirical upper bound.

Method 1	Method 2	p-value	Method 1	Method 2	p-value	Method 1	Method 2	p-value
LOF (0.1282)	iForest (0.1536)	0.3135	ME (0.1382)	ISAC (0.1658)	0.156	ISAC (0.1658)	EUB (0.2051)	0.0015
LOF (0.1282)	ME (0.1382)	0.433	ME (0.1382)	AS (0.1943)	0.0005	AS (0.1943)	SS (0.197)	0.9702
LOF (0.1282)	GB (0.1524)	0.4553	ME (0.1382)	SS (0.197)	0.0002	AS (0.1943)	ALORS (0.1728)	0.0206
LOF (0.1282)	ISAC (0.1658)	0.1005	ME (0.1382)	ALORS (0.1728)	0.009	AS (0.1943)	MetaOD_C (0.198)	0.8446
LOF (0.1282)	AS (0.1943)	0.0025	ME (0.1382)	MetaOD_C (0.198)	0.0008	AS (0.1943)	MetaOD_F (0.1966)	0.3135
LOF (0.1282)	SS (0.197)	0.0045	ME (0.1382)	MetaOD_F (0.1966)	0.0012	AS (0.1943)	MetaOD (0.2035)	0.2959
LOF (0.1282)	ALORS (0.1728)	0.062	ME (0.1382)	MetaOD (0.2035)	0.0004	AS (0.1943)	EUB (0.2051)	0.0304
LOF (0.1282)	MetaOD_C (0.198)	0.001	ME (0.1382)	EUB (0.2051)	0.0004	SS (0.197)	ALORS (0.1728)	0.0003
LOF (0.1282)	MetaOD_F (0.1966)	0.01	GB (0.1524)	ISAC (0.1658)	0.7172	SS (0.197)	MetaOD_C (0.198)	0.8092
LOF (0.1282)	MetaOD (0.2035)	0.0013	GB (0.1524)	AS (0.1943)	0.0032	SS (0.197)	MetaOD_F (0.1966)	0.4553
LOF (0.1282)	EUB (0.2051)	0.0007	GB (0.1524)	SS (0.197)	0.0002	SS (0.197)	MetaOD (0.2035)	0.7938
iForest (0.1536)	ME (0.1382)	0.029	GB (0.1524)	ALORS (0.1728)	0.3703	SS (0.197)	EUB (0.2051)	0.099
iForest (0.1536)	GB (0.1524)	0.0365	GB (0.1524)	MetaOD_C (0.198)	0.0169	ALORS (0.1728)	MetaOD_C (0.198)	0.0276
iForest (0.1536)	ISAC (0.1658)	0.7369	GB (0.1524)	MetaOD_F (0.1966)	0.0111	ALORS (0.1728)	MetaOD_F (0.1966)	0.0137
iForest (0.1536)	AS (0.1943)	0.008	GB (0.1524)	MetaOD (0.2035)	0.0051	ALORS (0.1728)	MetaOD (0.2035)	0.0025
iForest (0.1536)	SS (0.197)	0.0012	GB (0.1524)	EUB (0.2051)	0.0008	ALORS (0.1728)	EUB (0.2051)	0.0006
iForest (0.1536)	ALORS (0.1728)	0.6274	ISAC (0.1658)	AS (0.1943)	0.0169	MetaOD_C (0.198)	MetaOD_F (0.1966)	0.7475
iForest (0.1536)	MetaOD_C (0.198)	0.0276	ISAC (0.1658)	SS (0.197)	0.0051	MetaOD_C (0.198)	MetaOD (0.2035)	0.6874
iForest (0.1536)	MetaOD_F (0.1966)	0.0276	ISAC (0.1658)	ALORS (0.1728)	0.6542	MetaOD_C (0.198)	EUB (0.2051)	0.1773
iForest (0.1536)	MetaOD (0.2035)	0.009	ISAC (0.1658)	MetaOD_C (0.198)	0.062	MetaOD_F (0.1966)	MetaOD (0.2035)	0.1165
iForest (0.1536)	EUB (0.2051)	0.001	ISAC (0.1658)	MetaOD_F (0.1966)	0.008	MetaOD_F (0.1966)	EUB (0.2051)	0.0251
ME (0.1382)	GB (0.1524)	0.0569	ISAC (0.1658)	MetaOD (0.2035)	0.0019	MetaOD (0.2035)	EUB (0.2051)	0.0522

G.2 Experiment Results for ST Testbed

We present the method performance in Table 7, and hypothesis test result in Table 8. Among all meta-learners, METAOD shows the best MAP.

Table 7: Method evaluation in ST testbed (average precision). The most performing method is highlighted in **bold**. The rank is provided in parenthesis (lower ranks denote better performance). METAOD achieves the best average precision and average rank among all meta-learners.

Datasets	LOF	iForest	ME	GB	ISAC	AS	SS	ALORS	MetaOD_c	MetaOD_F	RS	MetaOD
abalone	0.092 (10)	0.1654 (2)	0.1338 (6)	0.1584 (3)	0.15 (4)	0.1232 (9)	0.1688 (1)	0.1316 (7)	0.0737 (12)	0.1274 (8)	0.092 (10)	0.1355 (5)
ALOI	0.1424 (2)	0.0333 (6)	0.0284 (11)	0.0333 (6)	0.0329 (9)	0.5714 (1)	0.042 (4)	0.0282 (12)	0.0335 (5)	0.0297 (10)	0.0491 (3)	0.0333 (6)
anthyroid	0.1522 (11)	0.2828 (7)	0.3177 (6)	0.3399 (5)	0.397 (2)	0.8089 (1)	0.3634 (4)	0.2716 (8)	0.0608 (12)	0.196 (10)	0.2384 (9)	0.3724 (3)
Anthyroid2	0.1351 (2)	0.1198 (5)	0.1173 (6)	0.0998 (8)	0.1353 (1)	0.109 (7)	0.0998 (8)	0.127 (4)	0.0837 (11)	0.0715 (12)	0.1283 (3)	0.0998 (8)
Arrhythmia	0.7435 (5)	0.7615 (2)	0.6643 (9)	0.7622 (1)	0.7471 (4)	0.0478 (12)	0.7134 (8)	0.7252 (7)	0.3496 (11)	0.7273 (6)	0.3909 (10)	0.7606 (3)
arrhythmia2	0.3925 (9)	0.463 (4)	0.1833 (10)	0.4664 (2)	0.4239 (7)	0.0396 (12)	0.3949 (8)	0.4323 (5)	0.1833 (10)	0.4269 (6)	0.6772 (1)	0.4664 (2)
breastw	0.2822 (12)	0.9695 (3)	0.9716 (2)	0.9684 (4)	0.9564 (7)	0.3742 (11)	0.9504 (8)	0.9615 (6)	0.817 (9)	0.9741 (1)	0.8022 (10)	0.9632 (5)
Cardio	0.2802 (10)	0.4454 (4)	0.4418 (5)	0.4187 (7)	0.3299 (9)	0.2313 (12)	0.5306 (1)	0.2328 (11)	0.4989 (2)	0.4785 (3)	0.3611 (8)	0.4233 (6)
comm	0.1104 (2)	0.0418 (6)	0.0486 (3)	0.0251 (9)	0.0397 (7)	0.6461 (1)	0.073 (3)	0.0289 (8)	0.01 (12)	0.0153 (10)	0.0153 (10)	0.0509 (4)
concrete	0.0951 (3)	0.0502 (5)	0.0153 (12)	0.0455 (9)	0.0412 (10)	0.1347 (1)	0.0493 (6)	0.0217 (11)	0.0471 (8)	0.0493 (6)	0.1347 (1)	0.0508 (4)
fault	0.2064 (10)	0.4269 (4)	0.2114 (8)	0.4294 (3)	0.4364 (2)	0.1297 (12)	0.2136 (7)	0.4378 (1)	0.3838 (6)	0.1458 (11)	0.2114 (8)	0.389 (5)
gas	0.0265 (2)	0.0017 (4)	0.0016 (5)	0.0016 (5)	0.0018 (3)	0.1382 (1)	0.001 (8)	0.0009 (10)	0.0009 (10)	0.001 (8)	0 (12)	0.0016 (5)
glass	0.1388 (2)	0.0944 (8)	0.068 (11)	0.1033 (7)	0.1268 (4)	0.1318 (3)	0.1393 (1)	0.0812 (10)	0.0411 (12)	0.1183 (6)	0.0936 (9)	0.1231 (5)
Glass2	0.1436 (7)	0.2108 (2)	0.2066 (3)	0.1506 (5)	0.1506 (5)	0.1295 (9)	0.0916 (11)	0.0837 (12)	0.2301 (1)	0.1115 (10)	0.1301 (8)	0.2034 (4)
HeartDisease	0.4804 (9)	0.5306 (5)	0.5646 (1)	0.5412 (3)	0.5479 (2)	0.0517 (12)	0.5276 (6)	0.5172 (8)	0.4604 (11)	0.4667 (10)	0.5317 (4)	0.5204 (7)
Hepatitis	0 (11)	0.2388 (8)	0.3008 (2)	0.2527 (5)	0.2501 (6)	0.2842 (3)	0.259 (4)	0.2407 (7)	0.2012 (10)	0 (11)	0.2388 (8)	0.329 (1)
impseg	0.1062 (12)	0.3506 (5)	0.3635 (3)	0.3485 (7)	0.3498 (6)	0.4699 (1)	0.2688 (8)	0.3552 (4)	0.1766 (11)	0.1844 (9)	0.1844 (9)	0.3742 (2)
InternetAds	0.2557 (10)	0.5101 (1)	0.4136 (5)	0.4431 (2)	0.3385 (8)	0.0097 (12)	0.419 (4)	0.3858 (6)	0.3714 (7)	0.2173 (11)	0.3288 (9)	0.4431 (2)
ionosphere	0.7949 (4)	0.81 (2)	0.357 (10)	0.7866 (5)	0.3474 (11)	0.2536 (12)	0.81 (2)	0.7858 (6)	0.565 (9)	0.6354 (8)	0.6885 (7)	0.8316 (1)
landsat	0.1561 (2)	0.1291 (9)	0.0941 (10)	0.1325 (6)	0.1314 (8)	0.1628 (1)	0.1365 (3)	0.1325 (6)	0.0941 (10)	0.1326 (5)	0.0941 (10)	0.1336 (4)
letter	0.4889 (3)	0.0866 (10)	0.547 (2)	0.0811 (11)	0.201 (6)	0.6958 (1)	0.1194 (8)	0.0951 (9)	0.0992 (12)	0.3901 (4)	0.1682 (7)	0.3658 (5)
letter	0.2038 (1)	0.0967 (10)	0.1606 (2)	0.0972 (8)	0.0981 (7)	0.0073 (11)	0.1355 (4)	0.0983 (6)	0.1554 (3)	0.0969 (9)	0.0073 (11)	0.1193 (5)
lympho	0.7817 (8)	1 (1)	0.8968 (7)	0.9762 (4)	0.6762 (10)	0.2054 (12)	0.9333 (6)	0.9444 (5)	0.753 (9)	1 (1)	0.6471 (11)	1 (1)
magic	0.1143 (8)	0.1516 (4)	0.1219 (7)	0.1459 (5)	0.1568 (2)	0.2403 (1)	0.1104 (9)	0.1352 (6)	0.0866 (11)	0.0479 (12)	0.1096 (10)	0.155 (3)
mammography	0.0793 (11)	0.2178 (2)	0.1206 (10)	0.1783 (4)	0.1744 (6)	0.0229 (12)	0.1609 (8)	0.1759 (5)	0.3414 (1)	0.1537 (9)	0.1692 (7)	0.2033 (3)
mmist	0.2211 (7)	0.2435 (4)	0.1589 (9)	0.2421 (5)	0.1096 (10)	0.0982 (11)	0.3418 (2)	0.2635 (3)	0.0785 (12)	0.1787 (8)	0.2333 (6)	0.4136 (1)
mnist	0.0662 (12)	0.9147 (7)	0.9994 (3)	0.9994 (6)	0.9996 (2)	0.1654 (11)	0.4462 (10)	0.8162 (8)	0.9994 (3)	1 (1)	0.6592 (9)	0.9992 (2)
opt.digits	0.0764 (2)	0.0673 (2)	0.0609 (8)	0.0664 (5)	0.0664 (5)	0.0607 (9)	0.0673 (3)	0.0588 (11)	0.0594 (12)	0.0619 (7)	0.0822 (1)	0.0619 (7)
opt.digits	0.0321 (8)	0.0449 (6)	0.0222 (10)	0.0639 (1)	0.0433 (7)	0.0619 (2)	0.0274 (9)	0.0617 (3)	0.0222 (10)	0.0515 (5)	0.053 (4)	0.0219 (12)
pageb	0.3763 (8)	0.458 (5)	0.3615 (9)	0.4594 (3)	0.4377 (7)	0.357 (10)	0.4594 (3)	0.4813 (1)	0.1635 (11)	0.1092 (12)	0.4813 (1)	0.458 (5)
PageBlocks	0.2861 (9)	0.495 (2)	0.2654 (10)	0.4596 (5)	0.4767 (4)	0.2333 (11)	0.5039 (1)	0.4787 (3)	0.2288 (12)	0.4202 (7)	0.3944 (8)	0.4538 (6)
particle	0.0633 (8)	0.0724 (4)	0.0564 (9)	0.0841 (2)	0.0668 (7)	0.2732 (1)	0.0671 (6)	0.0519 (10)	0.0439 (11)	0.0677 (5)	0.0439 (11)	0.0768 (3)
PenDigits	0.0999 (5)	0.0048 (7)	0.094 (3)	0.005 (6)	0.0031 (9)	0.5355 (1)	0.0016 (4)	0.0015 (10)	0.0012 (11)	0.0012 (11)	0.1661 (2)	0.0045 (8)
pendigits2	0.0528 (9)	0.2013 (4)	0.1143 (5)	0.2843 (1)	0.0892 (6)	0.0127 (12)	0.0789 (7)	0.263 (2)	0.0414 (10)	0.063 (8)	0.0134 (11)	0.2236 (3)
pinna	0.4239 (10)	0.5139 (2)	0.4044 (11)	0.4674 (6)	0.4674 (6)	0.1632 (12)	0.4504 (8)	0.5073 (3)	0.5586 (1)	0.4499 (9)	0.4678 (5)	0.505 (4)
Pinna2	0.4606 (8)	0.5175 (4)	0.6371 (11)	0.4874 (6)	0.4467 (9)	0.0511 (12)	0.5314 (2)	0.5097 (5)	0.5254 (3)	0.4446 (10)	0.4699 (7)	0.5434 (1)
satellite	0.3647 (11)	0.6745 (1)	0.6131 (5)	0.6315 (4)	0.5931 (7)	0.5675 (10)	0.6082 (6)	0.6697 (2)	0.3571 (12)	0.5757 (8)	0.5729 (9)	0.6515 (3)
satimage-2	0.0332 (10)	0.9217 (3)	0.7552 (8)	0.9303 (1)	0.8964 (5)	0.0241 (11)	0.8457 (7)	0.9167 (4)	0.0096 (12)	0.8479 (6)	0.6211 (9)	0.9296 (2)
satimage	0.2052 (11)	0.2249 (5)	0.3363 (2)	0.2282 (4)	0.2232 (7)	0.3736 (1)	0.2249 (5)	0.2413 (3)	0.1146 (12)	0.2209 (9)	0.2232 (7)	0.2143 (10)
shuttle2	0.0981 (9)	0.972 (3)	0 (12)	0.9724 (1)	0.9724 (1)	0.4726 (5)	0.1199 (8)	0.4726 (5)	0.3588 (6)	0.0426 (10)	0.1532 (7)	0.0418 (11)
Shuttle3	0.3512 (2)	0.0806 (6)	0.2628 (4)	0.0648 (8)	0.0715 (7)	0.5834 (1)	0.047 (11)	0.0479 (10)	0.0126 (12)	0.1266 (5)	0.0648 (8)	0.3481 (3)
skin	0.1102 (4)	0.0972 (8)	0.1538 (1)	0.1003 (7)	0.1056 (5)	0.066 (12)	0.1156 (3)	0.0761 (9)	0.1538 (1)	0.076 (11)	0.0761 (9)	0.1007 (6)
smtp_n	0.0012 (10)	0.0046 (7)	0.0035 (8)	0.0074 (5)	0.0087 (4)	0.6709 (1)	0.0004 (6)	0.0455 (3)	0 (11)	0 (11)	0.0035 (8)	0.2227 (2)
spambase	0.012 (9)	0.0238 (4)	0.0036 (10)	0.0228 (5)	0.0248 (3)	0.3843 (2)	0.0176 (8)	0.0189 (6)	0.0036 (10)	0.0036 (10)	0.4243 (1)	0.0189 (6)
Spambase2	0.3516 (10)	0.4666 (7)	0.3029 (11)	0.4654 (8)	0.4842 (6)	0.5261 (4)	0.5369 (1)	0.5283 (2)	0.3015 (12)	0.3802 (9)	0.5283 (2)	0.505 (5)
speech	0.0284 (3)	0.0193 (9)	0.0324 (2)	0.0246 (5)	0.0147 (11)	0.024 (6)	0.0213 (8)	0.0158 (10)	0.0134 (12)	0.0987 (1)	0.023 (7)	0.0281 (4)
Stamps	0.1453 (12)	0.3326 (2)	0.1569 (10)	0.2957 (5)	0.2856 (7)	0.1532 (11)	0.3383 (1)	0.2948 (6)	0.2411 (9)	0.3006 (3)	0.2812 (8)	0.2982 (4)
synthetic	0.1552 (1)	0.1192 (5)	0.1477 (2)	0.1197 (4)	0.113 (7)	0.0938 (11)	0.0986 (9)	0.0974 (10)	0.1032 (8)	0 (12)	0.1192 (5)	0.1464 (3)
thyroid	0.0356 (11)	0.6295 (6)	0.7751 (1)	0.6054 (7)	0.3558 (8)	0.0603 (9)	0.732 (3)	0.697 (4)	0.0265 (12)	0.7751 (1)	0.0603 (9)	0.6677 (5)
vertebral	0.1135 (3)	0.0917 (9)	0.0918 (8)	0.0925 (7)	0.0996 (6)	0.6885 (1)	0.0877 (11)	0.0856 (12)	0.0998 (5)	0.1175 (2)	0.1052 (4)	0.0887 (10)
vowels	0.3005 (4)	0.1679 (5)	0.3438 (3)	0.0997 (8)	0.0754 (9)	0.1031 (7)	0.8841 (1)	0.1452 (6)	0.0193 (11)	0.0279 (10)	0.0193 (11)	0.6355 (2)
wave	0.0479 (3)	0.0128 (7)	0.01 (10)	0.0115 (9)	0.0124 (8)	0.3835 (1)	0.0479 (3)	0.0479 (3)	0.0557 (2)	0.0076 (12)	0.01 (10)	0.0239 (5)
Waveform	0.0834 (4)	0.0593 (8)	0.1306 (3)	0.0543 (9)	0.0537 (10)	0.4882 (1)	0.0478 (12)	0.051 (11)	0.2756 (2)	0.0596 (7)	0.0659 (5)	0.064 (6)
wbc	0.5394 (8)	0.5783 (6)	0.6497 (1)	0.594 (2)	0.5226 (9)	0.0503 (12)	0.3401 (10)	0.5736 (7)	0.0989 (11)	0.5853 (5)	0.594 (2)	0.594 (2)
WBC2	0.1038 (9)	0.8643 (1)	0.0283 (10)	0.8562 (2)	0.7213 (3)	0.2639 (8)	0.0283 (10)	0.3856 (7)	0.0283 (10)	0.6586 (5)	0.6575 (6)	0.6613 (4)
WDBC	0.729 (1)	0.6773 (4)	0.6699 (5)	0.6449 (8)	0.6962 (3)	0.4283 (11)	0.7252 (2)	0.6579 (7)	0.1268 (12)	0.6202 (9)	0.5957 (10)	0.6622 (6)
Wilt	0.1001 (2)	0.0485 (7)	0.0602 (5)	0.0402 (11)	0.0446 (9)	0.6381 (1)	0.0653 (3)	0.0485 (7)	0.0446 (9)	0.0644 (4)	0.0495 (6)	0.0402 (11)
wine	0.0066 (12)	0.0091 (8)	0.0127 (3)	0.0107 (4)	0.0092 (7)	0.644 (1)	0.0085 (9)	0.0101 (6)	0.0075 (10)	0.0075 (10)	0.2477 (2)	0.0103 (5)
wine2	0.176 (8)	0.2442 (4)	0.1108 (9)	0.2008 (5)	0.3074 (3)	0.3818 (2)	0.0745 (10)	0.1832 (6)	0.0536 (12)	0.0571 (11)	0.1832 (6)	0.8697 (1)
WPBC	0.2317 (9)	0.2311 (10)	0.2363 (5)	0.223 (12)	0.2487 (2)	0.3333 (1)	0.2487 (2)	0.2318 (8)	0.2277 (11)	0.2358 (6)	0.2329 (7)	0.2465 (4)
yearp	0.4978 (1)	0.4922 (4)	0.4937 (2)	0.4921 (5)	0.4805 (10)	0.2076 (12)	0.4877 (9)	0.4901 (7)	0.4758 (11)	0.4905 (6)	0.4937 (2)	0.4881 (8)
yeast	0.0596 (7)	0.058 (9)	0.0561 (12)	0.0586 (8)	0.064 (5)	0.1227 (1)	0.0675 (2)	0.0637 (6)	0.0576 (10)	0.0575 (11)	0.0675 (2)	0.0672 (4)
Average	0.2154 (6.87)	0.3197 (5.08)	0.2689 (6.44)	0.3137 (5.42)	0.2892 (6.13)	0.2704 (6.53)	0.2814 (5.73)	0.2981 (6.6)	0.1946 (8.97)	0.2594 (7.68)	0.2582 (6.9)	0.3382 (4.53)
STD	0.2027	0.2967	0.2602	0.2966	0.2712	0.221	0.2691	0.2839	0.2199	0.2813	0.2268	0.2882

Table 8: Pairwise statistical test results between METAOD and baselines by Wilcoxon signed rank test in ST. Statistically better method shown in **bold** (both marked **bold** if no significance). METAOD related pairs are surrounded by rectangles. METAOD achieves the highest MAP and best average rank, and statistically significantly better than all baselines except iForest.

Method 1	Method 2	p-value	Method 1	Method 2	p-value	Method 1	Method 2	p-value
LOF (0.2154)	iForest (0.3197)	0.0032	ME (0.2689)	ISAC (0.2892)	0.6817	ISAC (0.2892)	MetaOD (0.3382)	0.0006
LOF (0.2154)	ME (0.2689)	0.5258	ME (0.2689)	AS (0.2704)	0.9525	AS (0.2704)	SS (0.2814)	0.8471
LOF (0.2154)	GB (0.3137)	0.01	ME (0.2689)	SS (0.2814)	0.2345	AS (0.2704)	ALORS (0.2981)	0.5725
LOF (0.2154)	ISAC (0.2892)	0.1016	ME (0.2689)	ALORS (0.2981)	0.5031	AS (0.2704)	MetaOD_C (0.1946)	0.0667
LOF (0.2154)	AS (0.2704)	0.1683	ME (0.2689)	MetaOD_C (0.1946)	0.0026	AS (0.2704)	MetaOD_F (0.2594)	0.6112
LOF (0.2154)	SS (0.2814)	0.0575	ME (0.2689)	MetaOD_F (0.2594)	0.2389	AS (0.2704)	RS (0.2582)	0.8622
LOF (0.2154)	ALORS (0.2981)	0.0461	ME (0.2689)	RS (0.2582)	0.3672	AS (0.2704)	MetaOD (0.3382)	0.0009
LOF (0.2154)	MetaOD_C (0.1946)	0.0345	ME (0.2689)	MetaOD (0.3382)	0.0001	SS (0.2814)	ALORS (0.2981)	0.7604
LOF (0.2154)	MetaOD_F (0.2594)	0.6176	GB (0.3137)	ISAC (0.2892)	0.0849	SS (0.2814)	MetaOD_C (0.1946)	0.0001
LOF (0.2154)	RS (0.2582)	0.1735	GB (0.3137)	AS (0.2704)	0.4468	SS (0.2814)	MetaOD_F (0.2594)	0.0069
LOF (0.2154)	MetaOD (0.3382)	0.0001	GB (0.3137)	SS (0.2814)	0.5412	SS (0.2814)	RS (0.2582)	0.1419
iForest (0.3197)	ME (0.2689)	0.0484	GB (0.3137)	ALORS (0.2981)	0.1002	SS (0.2814)	MetaOD (0.3382)	0.0190
iForest (0.3197)	GB (0.3137)	0.047	GB (0.3137)	MetaOD_C (0.1946)	0.0001	ALORS (0.2981)	MetaOD_C (0.1946)	0.0001
iForest (0.3197)	ISAC (0.2892)	0.0127	GB (0.3137)	MetaOD_F (0.2594)	0.0001	ALORS (0.2981)	MetaOD_F (0.2594)	0.0280
iForest (0.3197)	AS (0.2704)	0.3714	GB (0.3137)	RS (0.2582)	0.0017	ALORS (0.2981)	RS (0.2582)	0.0054
iForest (0.3197)	SS (0.2814)	0.1942	GB (0.3137)	MetaOD (0.3382)	0.0030	ALORS (0.2981)	MetaOD (0.3382)	0.0021
iForest (0.3197)	ALORS (0.2981)	0.0012	ISAC (0.2892)	AS (0.2704)	0.7233	MetaOD_C (0.1946)	MetaOD_F (0.2594)	0.0342
iForest (0.3197)	MetaOD_C (0.1946)	0.0001	ISAC (0.2892)	SS (0.2814)	0.9513	MetaOD_C (0.1946)	RS (0.2582)	0.0115
iForest (0.3197)	MetaOD_F (0.2594)	0.0001	ISAC (0.2892)	ALORS (0.2981)	0.9357	MetaOD_C (0.1946)	MetaOD (0.3382)	0.0001
iForest (0.3197)	RS (0.2582)	0.0012	ISAC (0.2892)	MetaOD_C (0.1946)	0.0003	MetaOD_F (0.2594)	RS (0.2582)	0.4616
iForest (0.3197)	MetaOD (0.3382)	0.1129	ISAC (0.2892)	MetaOD_F (0.2594)	0.0159	MetaOD_F (0.2594)	MetaOD (0.3382)	0.0001
ME (0.2689)	GB (0.3137)	0.1002	ISAC (0.2892)	RS (0.2582)	0.0344	RS (0.2582)	MetaOD (0.3382)	0.0001